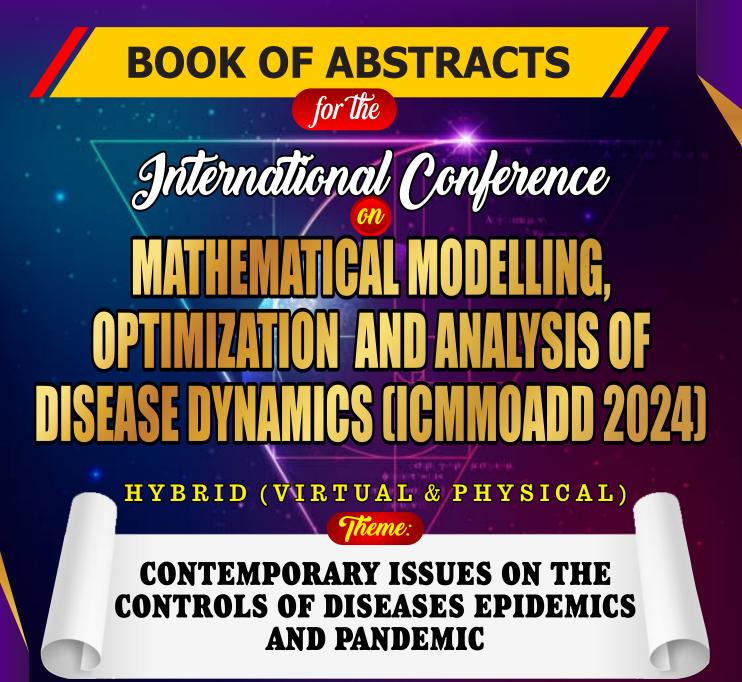




# MATH MODEL RESEARCH GROUP DEPARTMENT OF MATHEMATICS FEDERAL UNIVERSITY OF TECHNOLOGY (FUT), MINNA, NIGERIA



DATE: Thursday 22nd February, 2024 TIME: 10:00am Prompt VENUE: Department of Mathematics, Federal University of Technology Minna, Nigeria

> PROFESSOR N. I. AKINWANDE FNMS Convener

B7: Numerical Solutions of Higher Order Differential Equations via New Iterative Method - **Khadeejah James Audu** 36

B8: The Effect of a Source Term Inflow and Shockwaves Evaluation on Traffic Flow Model for a Single-Lane Highway - **A. Hamisu and D.M. Auwal** 36

B9: Dynamic Buckling Load of a Quadratic Model Structure with Nonlinear and Linear Damping under a Step Load - Gerald E. Ozoigbo 37

B10: Numerical Method to Minimize Tumor Density and Drug Side Effect in Cancer Treatment Regimen - Adamu, S. and Odekunle, M. R. 37

B11: Analysis of Magnetohydrodynamic Oscillatory Flow with Viscous Energy Dissipation -H. O. Adebayo, R. O. Olayiwola and T. J. Akintaro 38

B12: Heat and Mass Transfer Flow in a Channel Filled with Porous Medium in the Presence of Variable Thermal Conductivity - I. H. Kaita, S. Y. Zayyanu, L. Mas'ud, U. Abdullahi 39

B13: The Effect of a Source Term Inflow and Shockwaves Evaluation on Traffic Flow Model for a Single-Lane Highway - Aminu Hamisu, Zulkifilu Mu'azu and Dajuma Muhammad Auwal 39

B14: Numerical Solution for Magnetohydrodynamics Mixed Convection Flow Near a Vertical Porous Plate under the Influence of Magnetic effects and Velocity Ratio - **Ibrahim Yusuf**, **Umaru Mohammed and Khadeejah James Audu** 40

B15: Analytical Study of Temperature–Dependent Thermal Conductivity in Convective Drying of Food Material - Zhiri, A. B. and Ugwu, U. C. 41

B16: Mathematical Analysis of Wood Pyrolysis and Combustion - Yisa, E. M., Olayiwola R.O., Adamu, A.A., Cole, A.T.

B17: Analytical Investigation of Thermal Stratification in the Flow of Fluid in a CylindricalPipe - H. M. Yahaya, S. I. Yusuf and O. R. Jimoh42

B18: Effect of Heat Source with Convective Surface boundary condition on MHD Heat and Mass Transfer of Chemical Reaction Flow for a Moving Vertical Plate - D. M. Auwal., M. M. Gafai
 42

B19: Derivation and Implementation of a-Stable Hybrid Block Numerical Method for Solving Stiff Ordinary Differential Equations - Alhassan Buhari, Musa Hamisu, Ismail Muhammad Musa, Hamza Yusuf 43

B20: Studying the Impact of Some Thermal Properties in Mhd Fluids on Heat and Mass
Transport Flow Within a Plate Embedded with Radiation and Heat Source - Ugwu U. C.,
Egbugha M. C., Adedayo O. A., and Zhiri A. B.

B21: Analytical Approximation solution for Integro Delay Differential Equation - Aminu Barde and Ahmad Banji Jafar 44

## **B19:** Derivation and Implementation of a-Stable Hybrid Block Numerical Method for Solving Stiff Ordinary Differential Equations

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## Abstract

A new 2-point hybrid block method for the numerical solution of first-order stiff systems of ordinary differential equations in initial value problems with optimal stability property is presented. The necessary and sufficient conditions for the convergence of the proposed implicit block numerical scheme for solving stiff ODEs are established. The stability and convergence analysis of the method show that it is consistent, zero-stable, and convergent. The absolute stability region of the method is plotted, indicating that the method is A-stable. The method is implemented in Microsoft Dev C++ environment using the C programming language and Newton's iteration, and some selected first-order stiff initial value problems are solved. The numerical results obtained for the proposed method are compared with the existing fully implicit 2-point block backward differentiation formula and 2-point block backward differentiation formula with two off-step points methods. The comparison reveals that the new method outperforms both methods in terms of accuracy and computation time as we reduce the step size. It is evident that the method converges faster.

**Keywords**: A-stable, hybrid block method, Stiff IVPs, Convergence and Block Backward Differentiation Formula.

# **B20:** Studying the Impact of Some Thermal Properties in Mhd Fluids on Heat and Mass Transport Flow Within a Plate Embedded with Radiation and Heat Source

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## Abstract

This research investigates the impact of certain thermo-physical properties of a fluid on the flow of heat and mass transfer through free convection. The fluid in consideration is a chemically reacting, viscous, incompressible, and electrically conducting substance flowing past an infinite porous plate. The process is influenced by a uniform transverse magnetic field, with the fluid being optically thin, allowing the modeling of thermal radiative heat loss through the Rosseland approximation. A uniform magnetic field is applied perpendicularly to the plate,

and the fluid experiences a normal suction velocity, while the heat flux at the plate remains constant. The study involves solving the dimensionless partial differential equations governing the phenomenon through analytical methods, specifically employing the Olayiwola Generalized Polynomial Approximation Method (OGPAM). The obtained results illustrate the influence of various thermo-physical parameters on fluid flow, as well as heat and mass transfer characteristics, presented graphically. Skin-friction coefficient and Nusselt number values at the plate are numerically derived and discussed for different physical parameter values, presented in tables. The research also explores the effects of a generating heat source on fluid velocity and temperature, revealing that an increase in thermal radiation amplifies both the velocity and temperature profiles of the flow, thereby intensifying the convective flow.

**Keywords:** Convective flow, Heat and mass transfer, Heat source, MHD free convection, Porous medium, Thermal radiation, Unsteady flows.

## **B21:** Analytical Approximation solution for Integro Delay Differential Equation

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## Abstract

Delay Differential equations (DDEs) are types of functional equation having a wide range of application in the arena of sciences and engineering. Over the years, the application of these equations had shown in control theory and recently in various biological models. However, several techniques have experienced difficulties in finding a convergent approximate analytical solution of certain types of these equations. Therefore, in this work, the He-Natural Homotopy Analysis Method is used for analytical treatment of integro delay differential equation. The method is a blend of Natural transform and Homotopy analysis method. Based on this approach the Solution of this equation is given in form of rapid convergent series where the He's polynomial is used for series calculation of nonlinear terms. Hence, the result indicates that method is analytically efficient for handling such type of DDEs.