# COMPUTER SOLUTION TO PRODUCTION MODELING IN A MANUFACTURING COMPANY <br> (A CASE STUDY OF NIGERIAN BOTTLING COMPANY, Ilorin) 

## BY

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## ABSTRACT

The need to plan production is of utmost importance to the management of any manufacturing outfit. Efforts geared at computerizing analysis that can aid such planning are hence worthwhile. This project is one such effort.

This work is a successful attempt at computerizing time series analysis and forecasting of production data. The software, developed in Qbasic, can analyze any monthly time series data and produce forecasts and hence, not restricted to production data alone. The software exploits the highly interactive nature of Qbasic language and is user-friendly.

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## CERTIFICATION

We, the undersigned certify that this project was carried out by Odede, B. T. of the Department of Mathematics \& Computer Science, Federal University of Technology, Minna, Nigeria.

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# CHAPTER ONE <br> <br> GENERAL INTRODUCTION 

 <br> <br> GENERAL INTRODUCTION}

### 1.1 Introduction

In any profit oriented outfit, the need to meet customers' taste and demand at the appropriate time is uppermost in the minds of managers.

Gone were those days when planning was based on the rule of thumb. These days, planning process is essentially based on carefully analyzed data. Results of such analysis are usually in numerical terms and as such can be numerically and precisely interpreted. It is not just enough to say that the price of an item rises every January, but of interest in addition to this is by how much or by what percentage?

This will definitely create room for comparison with prices of other goods and hence places the investor in a better position as regards which items to invest on. In a similar manner, it is equally not enough to say that the demand for coca-cola increases during the dry season. Although, this is informative to the management of the company, it will be in the company's best interest if such can be put in numerical term so that such knowledge of the expected demand will help in future production planning.

To evolve such quantitative description, an attempt must be made at describing the movements of the series from time to
process, one can now project into the future. This is forecasting.

Since planning is critical to the success of any organization, it must be based on figures that are reliable. Reliable in the sense that the raw data must be reliable and the method of analysis must be correct so that results produced can be worth planning with. The reliability of such produced results will in turn depend on wether factors that influenced the pattern of the collected figures will behave alike within the period covered by the planning process.

It is worth mentioning that drastic changes in government policies can have drastic effects on planning as projected results may end up not being realized. There is always little or nothing managements of private organizations can do about this. Options available to such managements are not within the scope of this work.

This has been mentioned to forestall a situation whereby the software will be condemned on the basis that projected figures are much different from realized figures. All things being equal, the software will produce good and reliable results.

Although, production data generated by Nigeria Bottling Company will be used in test running the software, this does not mean that its use is restricted to Nigeria Bottling Company alone. In fact it is not even restricted to production data alone, rather it can be utilized by any one wishing to

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A project submitted to the Department of Mathematics and Computer Science, Federal University of Technology, Minna in partial fulfilment of the requirements for the award of Post-Graduate Diploma in Computer Science
have a better understanding of his monthly time series data with the ultimate aim of forecasting future values. Thus the software should be of interest to any organization that generates monthly data.

### 1.2 Scope and Limitations

The data collected covered a period of seven years, i.e (1990-1996) and the software can be used by any one wether individual or corporate willing to perform time series analysis on monthly data.

The software can not perform analysis on quarterly data except for minor adjustments are made. The software is only restricted to time series analysis on monthly basis and cannot be used on data collected on basis of longer time periods like quarters, six monthly, yearly etc.

### 1.3 Aims and Objectives

The main aim of this work is to develop a software that can be used to carry out time series analysis. That is the software should be able to decompose a time series into its various components.

The main objectives of the work are :
i) Fitting the annual trend equation to the monthly data collected.
ii) Conversion of fitted annual equation to monthly equation so that monthly trend projections can be made.
iii) Estimation of the seasonal component via computation of the seasonal index.
iv) Production of forecasts on the basis of trend and seasons estimates.

## CHAPTER TWO

## METHODOLOGY

### 2.1 Components of Time Series

A time series is a set of quantitative data collected sequentially in time i.e observations obtained at regular periods over a period of time. Such time period could be daily, weekly, monthly, yearly, etc. So students' enrolments at the Federal University of Technology, Minna over say eight years constitute a time series. Other examples include annual non-oil exports by Nigeria over years, monthly sales of beer oy a brewing company etc. One thing that these three examples have in common is that they are time dependent i.e they are all described with respect to time and hence the name time series.

All time series are expected to assume varying figures from time to time. Some factors are obviously responsible for the fluctuations. These factors are referred to as components of time series. Precisely, a time series is regarded as the result of the interaction of these components. These components are namely trend, seasonal, cyclical and random or irregular components.

Trend Component : This is the overall or persistent long-term, upward or downward pattern of movements. Such movements could be due to technological changes, changes in population, values, etc. Its duration is several years.

Seasonal Component : These are fairly regular periodic fluctuations which occur within each 12 -month period, year after year. Causes include weather conditions, social customs, religious customs, etc. Its duration is usually within twelve months.

Cyclical Component : These are repeating up and down swings or movements through four phases i.e from peak (prosperity) to contraction (recession) to depression to expansion or recovery. Its duration is usually two to ten years with differing intensity for a complete cycle.

Irregular Component : These are erratic or residual fluctuations which exist in a time series after taking into account the three other components. They do not occur with any statistical regularity. Its occurrence is due to unforeseen events like fire outbreak, war, strike, earthquake, etc.

### 2.2 Time Series Analysis

Time series analysis is the isolation of the components of the series so that the effect of each component can be measured. The analysis is based on one fundamental assumption that factors which affected the series under study during the period covered by the series will continue to behave in more or less the same manner in the future. So, if a forecast is being made, the analysis is assuming that the policies particularly as they affect the series remain fairly stable. Time series analysis has two perspectives. The first is
stationary time series analysis which utilizes Auto Regressive Integrated Moving Average (ARIMA) models for explaining the behaviour of time series. The second is the traditional approach which views the time series as either addition of its components (additive) or product of its components (multiplicative model).

In this work, the multiplicative model will be entertained. Usually when analyzing monthly data, attention is only paid to trend and seasonal effects for the purpose of explaining the behaviour of the series and forecasting.

In analyzing the trend, linear behaviour is always assumed for the series. The linear equation is given as

$$
T=a+b X+e
$$

where
$T$ is the dependent variable i.e the trend component of time series variable

X is the independent variable and it is the time variable
a is the intercept and it shows part of trend that is time independent.
b is the slope and it is the change in $T$ per unit change in X
$e$ is the error term
The parameters $a$ and $b$ of the linear model are estimated by least square estimation and the results are

$$
\begin{aligned}
b & =\frac{n \sum x y-\sum x \sum y}{\sum x^{2}-\left(\sum x\right)^{2}} \\
a & =\frac{\sum Y}{n}-\frac{b \sum X}{n}
\end{aligned}
$$

But if the coding is done such that

$$
\sum x=0
$$

then,

$$
b=\frac{\sum X Y}{\sum X^{2}}
$$

$$
a=\frac{\sum Y}{n}
$$

Since the software to be developed will code such that sumx $=0$, the latter versions of the estimates will be used.

The approach to be adopted in the trend fitting is to first sum figures for each year to get $T$, code the time variable accordingly and regress $T$ on $X$ to arrive at annual trend equation which is then converted to monthly equation accordingly.

If $a$ and $b$ are respectively the intercept and slope of the annual equation, then
i) for odd number of years, the monthly equation is

$$
T=\frac{a}{12}+\frac{b x}{144}
$$

ii) for even number of years, the monthly equation is

$$
T=\frac{a}{12}+\frac{b x}{72}
$$

Since we are interested in monthly forecast, one of these equations is used depending on whether the number of years is odd or even to estimate the trend. This trend estimate is subsequently combined with estimate of seasonal components to produce forecasts. The software will code the time variable accordingly, estimate the annual equation and convert it to monthly equation by making appropriate choice out of the two stated monthly equations.

The seasonal component is estimated by "seasonal index". It is the seasonal index that measures the fluctuation of series from month to month throughout a typical year. Seasonal index is defined as a set of numbers showing relative values of a variable during the months of the year. Twelve values expressed in percentages , each representing a month, constitute the seasonal index. Each figure is usually interpreted relative to monthly average.

For example, an index of $120 \%$ for the month of April
indicates that the series values for April are typically $20 \%$ higher than monthly average while $90 \%$ means $10 \%$ less than monthly average. Although, the Ratio- to-Moving Average method is the most tedious in terms of ease of calculation, it has been acclaimed the best and hence is to be used for estimating seasonal components. The steps involved are :
i) compute 12 -month moving total for the series
ii) compute 2 -month moving total of results from step (ii) iii) compute 12 -month centred moving average by dividing results from step(ii) by 24
iv) express original figure for each month as a percentage of the corresponding centred moving average
v) find the average percentages for corresponding months of different years using the mean
vi) express each mean from step (v) as a percentage of their own mean. The results constitute the required seasonal index.

Forecasting will be carried out by combining the monthly trend estimate and the corresponding index.

Forecast $=$ Trend x Seasonal index
Given the year and month for which forecast is desired, the software will produce forecast for 12 consecutive months starting from the month earlier indicated.

### 2.3 Time Series Models

Two models which fall within the class of traditional time series models are the additive model and the multiplicative model.

The additive model is given as

$$
Y=T+S+C+I
$$

and the multiplicative model is

$$
Y=T * S * C * I
$$

where:
Y is the time series variable
$T$ is the trend component
$S$ is the seasonal component
C is the cyclical component
I is the irregular component

## CHAPTER THREE

## LITERATURE REVIEW

### 3.1 General Review of Time Series Works

Time series works can be fundamentally divided into traditional time series modelling works (involving the multiplicative and additive models) and the Box-Jenkins approach (involving Autoregressive-Integrated -Moving Average (ARIMA) models).

Mark L.Berenson and David M.Levine (1986) treats elaborately, the traditional time series modelling with /special emphasis on the multiplicative model. They discussed meaningfully the methods of fitting trend including the moving average method, ordinary least squares approach, exponential smoothing and Holt-Winters approach to forecasting. Both the exponential smoothing and the Holt-Winters approaches are particular situations of the Box-Jenkins models. Instead of weighing all items equally as is done with moving average approach, exponential smoothing ensures that the weights assigned the values decrease with age so that the most recently observed value receives the highest weight, the previously observed value receives the next highest weight and so on, with the initially observed value receiving the lowest weight.

To smooth a series at any time period $t$, we require the following formula

$$
\boldsymbol{\epsilon}_{t}=W y_{t}+(1-W) \epsilon_{t-1}
$$

where
$\epsilon_{t}=$ value of the exponentially smoothedseries beig compute
$\epsilon_{t-1}=$ value of the exponentially smoothed series already col
$y_{t}=$ observed value of the time series $\in$ periodt

$$
\mathrm{w}=\text { subjectively assigned weight or smoothing }
$$ coefficient.

Note that $W+(1-W)=1$. Thus $W$ is a measure of relative emphasis placed on the current value os $y$ and what is left i.e (1-w) is a measure of relative emphasis placed on the exponentially weighted average of all previous values. i.e the lower $W$, the less relevant are past values of $y$; and the lower $W$, the more relevant are past $y$ values .

In relation to smoothing ability, a series of 1 term moving averages is related to an exponentially smoothed series having weight W as follows

$$
W=\frac{2}{1+2},
$$

Mark,L. Berenson and David, M. Levine (1986) and Richard, L.Mills (1977).

Thus smoothing a series by a moving average of order 1 is analogous to exponentially smoothing the series with smoothing constant $W=2 /(1+1)$. A moving average of order 3 is analogous to smoothing constant of 0.5 .

The following table gives some values of order of moving average,l and equivalent smoothing constant, W

| 1 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $W$ | .50 | .40 | .33 | .29 | .25 | .22 | .20 | .1 |

It is suggested that $W$ be kept at a small value (closer to 0) if the aim is to eliminate unwanted cyclical and irregular variations. If the aim is forecasting, $W$ is kept closer to 1.

Analysis of the seasonal effect is accomplished by computation of seasonal index. The Ratio-to-moving average method has enjoyed the greatest use owing to its superiority over others.

Murray.R.Spegiel (1981) and Mark.L.Berenson and David.M.Levine (1986) applied the method on monthly data on the basis of the multiplicative model.

Box and Jenkins (1876) discusses extensively what is now
generally referred to as Box-Jenkins approach to time series analysis. The approach is entirely different from traditional approach. The approach is built on the premise that many a time, values of frequently observed series at particular points in time are highly correlated with the values which precede and succeed them. The approach takes advantage of the potential autocorrelation feature inherent in the series.

This approach is described in steps below
i) postulate general class of models
ii) identify model to be tentatively entertained
iii) estimate parameters in the tentatively entertained model
iv) perform diagnostic checking
v) if model is adequate , go to step (vi) else, go to step (iii)
vi) use model for forecasting and control.

The general class can be represented in the form of the ARIMA model given as:

$$
\begin{equation*}
\phi(B)_{p} \nabla^{d} Z_{t}=\theta(B){ }_{q} a_{t} \tag{i}
\end{equation*}
$$

where :

$$
\phi(B)=\left(1-\phi_{1} B-\phi_{2} B^{2} \ldots \ldots \ldots-\phi p B^{p}\right)
$$

$$
\begin{aligned}
\theta(B) & =\left(1-\theta_{1} B-\theta_{2} B^{2}-\ldots \ldots \theta_{q} B^{q}\right) \\
a_{t} & \text { is a white noise process }
\end{aligned}
$$

$B$ is an operator defined by

$$
B^{j} Z_{t}=Z_{t-j}
$$

and

$$
\nabla=(1-B)
$$

d is the order of differencing required for stationarity.
$p$ and $q$ are the number of autoregressive and moving average parameters respectively.

If in (i), $p=0$ and $q=0$, we have a purely moving average process given by

$$
\nabla^{d} Z_{t}=\theta(B) a_{t} \quad \ldots \ldots \ldots(i i)
$$

If $q=0$ and $d=0$, we have a purely autoregressive process given by

$$
\nabla^{d} Z_{t} \phi(B)=a_{t} \quad \ldots \ldots \ldots(i i i)
$$

If $\mathrm{d}>0$ in (i), result is integrated moving average process

$$
Z_{t}=\theta(B) a_{t}
$$

If $d>0$ in (iii), result is integrated autoregressive process

$$
\phi(B) Z_{t}=a_{t}
$$

ARIMA model is written in short form as ARIMA ( $p, d, q$ ) where $p, d$ and $q$ remain as previously defined.
E.g for $p=0, d=1, q=1$ the resulting ARIMA model is $(0,1,1)$ process written as

$$
\begin{gathered}
\nabla Z_{t}=a_{t}-\theta_{1} a_{t-1} \\
(1-B) Z_{t}=a_{t}-\theta_{1} a_{t-1} \\
Z_{t}-Z_{t-1}=a_{t}-\theta_{1} a_{t-1} \\
\text { where }\left|\theta_{1}\right|<1
\end{gathered}
$$

for $p=0, d=2, q=2$, the resulting model is $\operatorname{ARIMA}(0,2,2)$ process written

$$
\begin{gathered}
\nabla^{2} Z_{t}=a_{t}-\theta_{1} a_{t-1}-\theta_{2} a_{t-2} \\
(1-B)^{2} Z_{t}=a_{t}\left(1-\theta_{1} B-\theta_{2} B^{2}\right) \\
\text { where } \theta_{1}+\theta_{2}<1
\end{gathered}
$$

$$
\theta_{1}+\theta_{2}<1
$$

$$
-1<\theta_{1}<1
$$

for $p=1, d=1, q=1$, we have $\operatorname{ARIMA}(1,1,1)$ process

$$
(1-B) \nabla Z_{t}=\left(1-\theta_{1} B\right) a_{t}
$$

$$
\text { where }-1<\theta_{1}<1,-1<\phi_{1}<1
$$

Box and Jenkins (1976) applied this approach on two hourly readings of 197 observations of a chemical process concentration and arrived at ARIMA $(0,1,1)$ process with parameter 0.7. i.e

$$
\nabla Z_{t}=(1-.7 B) a_{t}
$$

Application of the method on IBM stock of 369 observations resulted in ARIMA $(0,1,1)$ process with parameter -0.1. i.e

$$
\nabla Z_{t}=(1+.1 B) a_{t}
$$

Same analysis on 226 observations of a chemical process temperature resulted in ARIMA (1,1,0) process with parameter 0.8 i, e

$$
(1-.8 B) \nabla Z_{t}=a_{t}
$$

In recognition of the fact that monthly and quarterly data are often characterized by seasonal influences, Box and Jenkins incorporated seasonal factor into their ARIMA model. The seasonal ARIMA model is given as

$$
\phi(B)_{p} \Phi\left(B^{s}\right)_{P^{\nabla}} \nabla^{d}\left(\nabla^{D}\right)_{s} Z_{t}=\theta(B) \hat{v}\left(B^{s}\right) \ell_{\ell} a_{t}
$$

This model is said to be of order

$$
(p, d, q) \quad x \quad(P, D, Q)_{s}
$$

where :
$p$ is the number of non-seasonal autoregressive parameters
$P$ is the number of seasonal autoregressive parameters
s is seasonality and equals 12 for monthly data and
4 for quarterly data
$q$ is the number of non-seasonal moving average parameters
$Q$ is the number of seasonal moving average parameters

$$
z_{t} \text { is the time series }
$$

## $a_{t}$ 1s a white noise process

Box and Jenkins (1976) fitted ARIMA seasonal model to airline data and obtained seasonal model

$$
(0,1,1) \times(0,1,1)_{12}
$$

with parameters

$$
\theta=0.4, \quad \Phi=0.6
$$

The model is written as

$$
\begin{gathered}
\nabla \nabla_{12} z_{t}=(1-.4 B)(1-.6 B) a_{t} \\
\text { i.e } \quad z_{t}-z_{t-1}-z_{t-12}+z_{t-13}=a_{t}-.4 a_{t-1}-.6 a_{t-12}+.24 a_{t-13}
\end{gathered}
$$

### 3.2 Review of Computer solutions to Time Series Works

In recent years, the statistics profession has witnessed the development of a number of statistical software for use on various brands of microcomputers. Whereas in 1982 there were perhaps fewer than twenty microcomputer based statistical packages, by mid-1985, several hundreds packages were available, Mark and David (1986). Today, the number is outrageous.

Statistical packages are well defined integrated set of programs for performing various statistical analysis based on user's specifications using statistical technique, C.K. Ayo
(1994) .

Examples of statistical packages include
i) Statistical packages for social sciences (SPSS).
ii) Statistical analysis system (SAS).
iii) MYSTAT
iv) MINITAB
v) EXEC*U*STAT

These packages can handle the two distinct approaches to time series analysisin addition to numerous statistical analysis they can carry out. For example, SPSS has the ability to compute the autocorrelation function (ACF), the partial autocorrelation function (PACF), estimate parameters of ARIMA model and forecast. It can also carry out the traditional time series analysis by computing the trend and the seasonal index and hence forecast as desired.

Apart from these statistical packages like Lotus 1-2-3, Excel, Super-Calc can perform the trend analysis aspect of time series analysis if one supplies the appropriate tome codes. In fact the packages can handle fitting of autoregressive model (a class of ARIMA models) owing to their ability in multiple regression analysis.

In the absence of statistical packages, these spreadsheets can be used to analyze time series to some extent by creating formulas and using some of the predefined functions like MAX, MIN, SUM, AVG, etc

### 3.3 Relevance of Computer Application

Involvement of computer in area of application readily comes to mind when accuracy and speed are of much concern. These two concepts, accuracy and speed are mostly desired in statistical analysis generally. Researchers often have cause to analyze large volume of data. Handling such large volume of data manually has some drawbacks among which may be inaccuracy of results and rather slow processing speed and hence wasting of time.

Some of the computations are so involving that it will take the analyst a rather long time to complete the analysis. In time series, ARIMA modelling for example requires the computation of autocorrelation function, partial autocorrelation function, estimation of parameters and forecasting which involve very tedious calculations that no meaningful research work can be carried out in this area manually and accurate results obtained in good time. For instance, estimation of moving average parameters involves solving a system of equations which are non-linear in the parameters. This poses a problem if such is to be manually treated. Such situation obviously requires the intervention of computer. With available statistical packages, these otherwise complicated procedures have been reduced to very simple procedures.

In the traditional approach to time series, computation of seasonal index particularly, by the ratio-to-moving
average method can be cumbersome most especially for data on monthly basis collected for several years. Any mix-up in its computation will definitely affect the result. But with the existing statistical packages, the procedure has been simplified.

These days, researchers rarely encounter analysis problems as existing packages require just data definition and specification of the desired operation. These statistical packages remain very relevant owing to their contribution to speed of processing and accuracy. Their user friendliness makes them even more relevant.

## SYSTEM DESIGN

System design is the general and detailed specification of a computer based solution. Of crucial importance in system design is correct specification of the inputs to the system so that the garbage-in-garbage-out (GIGO) syndrome does not set in.

### 4.1 Input Description

The program consists of seven segments and hence inputs to the program shall be discussed on segment basis.

Segment 1: This segment prompts user to input "y" if he is a first time user of the software or "n" if not.

Segment 2: Prompts user for the number of years and "years" covered by data to be analyzed.

Segment 3: Prompts user for time series data.

### 4.2 Algorithm

An algorithm is defined as finite number of steps required for solving procedural problems. Flowchart will be used in presenting the algorithm for this work.

FLOWCHART



### 4.3 Program Description

Since the program is divided into segments, the description shall be on segment basis.

Segment 1: This marks the beginning of the program. It prompts the user to enter "y" if a first time user or "n" otherwise. If "y" is entered, some useful information about the software is displayed. If "n" is entered, the information is not displayed. If any other character besides " y " and "n" is entered, control is transferred back to the statement that prompts user to enter "y" or "n".

Segment 2: Prompts user for number of years covered by time series data . The program determines wether the number of years (n) is even or odd by checking wether (n/2-.5) is equal to integer part of $n / 2$. If (n/2-.5) is not equal to $n / 2$, then n is even else n is odd. This is necessary because choice of certain formulae in trend analysis depends on wether $n$ is even or odd. It also prompts user to enter the $n$ years e.g 1992, 1992, 1993, etc covered by data.

Segment 3: Prompts user to enter time series data. Data for whole year are accepted before the data for the following year. It displays each year and month for which data is required. The years displayed are years entered in segment 2. Segment 4: Computers sum and mean of data for each of $n$ years, assigns codes to the independent variable $X$ accordingly, computes the intercept and slope of the annual equation to monthly equation by computing the intercept and slope of
corresponding monthly equation. It makes a choice of the conversion formula to employ on the basis of wether the number of years is even or odd.

Segment 5: Computes 12-month moving total of original data, 2 month moving total of 12 -month moving total, divides results obtained by 24 to obtain 12 -month centred moving averages. Each set of original data is expressed as a percentage of corresponding 12 -month moving average. Results are averaged over corresponding months of different years and adjusted to give seasonal index.

Segment 6: Prompts user to enter year to forecast. It also requests user to enter any value from 1 to 12 January to December for first of months to forecast. Forecasts for 12 months first of which is month indicated are automatically are automatically computed.

Segment 7: Prints the original data, results of trend analysis, seasonal analysis, and forecasts

## CHAPTER FIVE

## SYSTEM IMPLEMENTATION

By system implementation, we mean placing the system into operation. On placing the system into operation, expected output and interpretation of results obtained are discussed below.

### 5.1 Output Expected

The program is expected to produce the following on execution.
i) Time series data entered
ii) Details of trend analysis
iii) Intercept and slope of fitted annual trend equation
iv) Intercept and slope of monthly trend equation
v) Details of seasonal analysis
vi) Seasonal index
vii) Forecasts

### 5.2 Interpretation of Results

The software has carried out three basic operations on the time series data. The three operations are trend analysis, seasonal analysis and forecasting.

The result of trend analysis reveals the following :
$Y=2200435-174581.5 X$
origin : 1993
X unit : 1 year
This equation suggests an annual decrease of about 174582 crates in production of coca-cola products.

The monthly trend equation is
$Y=183369.5-1212.372 X$
origin : July 1st 1993
X unit : 1 month
This equation suggests a monthly decrease of about 1212 crates in production of coca-cola products at Ilorin plant.

Results of the seasonal analysis reveal the following : Production in January is $9.8 \%$ greater than monthly average Production in February is 1.1\%lower than monthly average Production in March is 31.9\% greater than monthly average Production in April is $8.8 \%$ greater than monthly average Production in May is 11.9\% greater than monthly average Production in June is $4.0 \%$ less than monthly average Production in July is $16.2 \%$ less than monthly average Production in august is $18.9 \%$ less than monthly average Production in September is $28.3 \%$ less than monthly average Production in October is $22.0 \%$ less than monthly average Production in November is $5.2 \%$ greater than monthly average Production in December is $12.8 \%$ greater than monthly average

The forecasts are for January 1999-December 1999 and are only estimates based on the assumption that the production of coca-cola products will follow more or less the same pattern it followed during the period of 1990-1996. If this basic assumption is seriously violated, forecasts may be rendered useless.

### 5.3 Conclusion and Recommendations

In conclusion, the analysis carried out so far suggests that the coca-cola production at Ilorin plant has been decreasing at the rate of about 174582 crates annually. Such figure translates to monthly decrease of 1212 crates.

The seasonal analysis suggests that the production January, March, April, May, November and December are greater than monthly average while productions for the other months are less. The forecasts for 1999 suggest lower production than recorded in previous years.

It is recommended to the management of coca-cola to adopt more aggressive marketing strategy to arrest the downward trend in sales. It is recommended to interested researcher to go into software development for time series collected on annual basis.

Lastly, the software is recommended for use by anyone wishing to carry out time series analysis on time series data covering any number of years provided that such data are on monthly basis.

## REFERENCES

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COMPUTERIZED AFFROACH TO FRODUCTTON MODELLTNG IN A MANUFACTURING COMFANY GY Ddede，B．T．（Reg．No FGD／MCS／97／4ZZ）
Segment I：This segment gives some useful information to the fimst time use r＂Ame you a first time user of this softwame？（y／n）＂，oht

## PRINT \＃1，＂FRINT 排』，

TF cho＝＂y＂THEN 1 ELSE
INT \＃1，＂Information about the software＂
NT \＃ょ，
T \＃1，＂The software carries out timewseries analysis on montrly data＂
5 \＃1，＂based on the multiplicative model＂
$\Gamma$ \＃1，＂The software prompts you for the fiollowing＂
\＃1．＂＊number of years covered by your data＂
$\Gamma$ \＃3，＂＊years covered by your data e． $51995,1996,1997 "$
「\＃1，＂華 year \＆first of months（in terms of any integer value＂
「 \＃1，＂between 1－1e for jan＂－wee）whose forecests are desired．＂

「 \＃1，＂It automatically outputs foreceasts for le comsecutive months＂
r据＂stanting from the first month earlier indiceted＂
GOTD E
रEM Segment I：This segment aceepts preliminary datag dimensions some variables and assigns monthe
IT＂enter number of years covered by data＂n
＜ 3 THEN
FRINT＂number of years should not be less than 3 ＂
PRINT
GOTO E
IF
year（n）
$i=170 \mathrm{n}$
NPUT＂enter years covered by data e．g 1994． 1995 ete＂year（i）
i

index（1巳），amont $\$(1 已)$, forecast（le），trend（1E），avr（m）




Segment $2:$ accepts data
$i=1 \mathrm{TO} \mathrm{n}$
$R j=1 T 012$
READ SERIES（is $j$ ）
XT $j$
i
Segment 3：This segment computes row totals and means
$i=1 T 0 \mathrm{n}$
$a m(i\rangle=\theta$
i
$=\therefore T 0 \mathrm{n}$
＇$j=1$ TO גE
sum（i）$=\mathrm{msum}(i)+$ EERTES（i，j）
T j
i

```
jegment 4:
(i) =0
i
=1 T0 n
२j=1 T0 1E
=ot(i)=tot(i) + SERTES(i; j)
avm(i)=tot(i) / we
XT j
i
p$ = "e" THEN
(1) == (n-1)* (-1)
OR i = ETO n
x(i) = x(i - 1) +E
EXT i
        ELSE
} ={n - (1)* (-1.) /E
R i = ETO n
x(i) = x(i - - 1) + 1
EXT i
F
    =Q: total=Q: sumx< =#
    =1 TO n
i)}=x(i)*ttot(i
xy = sumxy + xy(i.)
al = total + tot(i)
xx = sumxx + x(i) * E
i
= total / n: byear = sumxy / 5um*x
p$ = "e" THEN
nth = ayear / 1E: bmonth = byear / 7e
    ELSE
onth = ayear / 1e: bmonth == byear / 144
F
Begment Sn This segment performes seasonal analysis
computation of de-month m.t;
    =1 TO F
bt(i)=0
i
= 1 70 f
j=1 TO 12
=1: c=j +=k-1
;F & \ IE THEN
        c=c - 1en i = i w i
    IF & > 1E GOTO 40
ND IF
k) = mtot(k) + SERIES(i, c)
T j
k
utation of E-month m.t of E-month m.t
=1 T0f-1
tot(i)=mtot(i) +mtot(i + 1)
(i) = movtot(i) / E4
i
ferring of semies into i-mim tr
= 1 T0 n
j = 1 TO 1E
= i > & THEN
k=\langlei-1\rangle* 12+j
        ELSE
i=j
```

```
trendx = (yea - origin) * 1E + (mont - 7)
trend(1) = (amonth + bmonth * .5) + (bmonth * tmendx)
forecast(1) = tremd(1) * imgex(mont) / 1ag
END IF
Segment G:This segment print 非ys the output
5 #1, TAR(z(a); "OUTFUT"
    F #1, TAR(30); "*******"
    r#1, = PRINT 非1,
    #, TAG(EG); "ORTGINAL VALUES"
    #1, TAR(EG); ".........................................."
: b=G
    =1TO E
    =11
    i =a TO b
ORINT #1, TAB(k); amomt$(i);
k=k+10
<T i
FOR i = 1 TO n
        k=1Q
        FRINT #&, TAR(E); year(i);
    FOR j = a TO E
        FRINT #1, TAR(k); SERTES(i, j);
        k=k+10
    NEXT j
\T i
```



```
    f
NT #s, : PRINT 非,, : FRTNT 非, 
NT 挑, TAB(ES); "TABLEE OF TREND AMALYSTS"
NT #1, TAB(巳S);
NT #1,
NT #1, TAR(13); "X"; TAR(巨g); "Y"; TAB(43); "XY"; TAB(5S); "XX"
    i = 1 T0 n
RINT #1, TAR(1E); x(i); TAE(ES); tot(i); TAR(4E); xy(i); TAE(57); x{i) ~ Z
i
NT #1; TAB(11); "total"# TAE(ES); totaly TAE{4E)" sumxy; TAE{5Z); sumx%
NT 排1, = FRINT 非&,
NT *s, "For the anmual equation"
NT #1, "Intercept: ="; ayeam
NT #1, "Slope ="; byear
NT #1, : PRINT #1.,
NT #1s "For the monthly equation"
VT #s, "Intercept ="; amonth
VT #1, "Slope ="; bmonth
VT #1, : PRINT #1.,
UT #1, TAR(ES): "CENTRED MDUTNG AUERAGE TARLE"
4T #1, TAB {巳S); "-...-..........................................................................."
NT #1, TAB(3); "YEAR"; TAE{11); "MONTH"; TAR{ES); "DATA"; TAB{32\; "1E-MTH
NT #&, TAB(47); "E --- MTH M.T OF C4";TGR(GG): "1E --. MTH CMA"
4T #1,
j=1 TO m
=1
i i = 1 TO 12
\prime=f+{j-1)*1E
RINT #1, TAR(E); year(j); TAR(1E); amomtu(i); TAR(ES); TR(D);
RINT #1, TAB{3E); MTOT1{D); TAE{49); MOUTOT1(D); TAE{GG): CMA1{D)
=f+1
Ti
j
T #1, : FRINT 非1,
```

Give ar
$T R(k)=$ SERTES $(i, j)$
XT $j$
i
nsfers mbot into mtoti
$i=1 \mathrm{TO} \mathrm{f}$
OTA（i $+G)=m \operatorname{tot}(i)$
i
nsfers contents of movtot into movtotd
$i=1 T 0 f-1$
UTOTI（i $+G)=$ movtot（i）
$A 1(i+G)=C M A(i)$
i
ides original values by oma
$i=1 T 0 f-1$

j
news ：dim c（n，1E）
TM Cm〈n，1こ〉
OR $i=1 \mathrm{TO} \mathrm{n}$
$\operatorname{FOR~} j=1$ TO IE

NEXT j
EXT i
5 values for corresponding months of diffement years
$i=1 \operatorname{ToL} \mathrm{~L}$
$r(i)=\square$
i
$j= \pm \operatorname{TO} n$
OR $j=1$ TO $1 E$
$\operatorname{per}(j)=\operatorname{per}(j)+\operatorname{mon}(i, j)$
cmean $(j)=\operatorname{per}\langle j\rangle /$（ $j$－-1 ）
IEXT j
T i
ustment of seasonal imolex
hean $=0$
$i=1 T 012$
otmean $=$ totmean + comean（i）
－
$\tan =$ totmean／ 12
$i=1 \mathrm{TO} 12$
idex $(i)=$ mean $(i) *$ dat avmean
$T$ i
Segment G：This segment performes forewesting
INFUT＂enter yr＂for＂which forecest is desimed＂，yea
INFUT＂enter btw 1 to $x=$ for jan＂dec for lst month to forecast＂＂mont
mont＜ 1 OR mont 〉 $1=$ THEN SR
INT \＃1，
IF typ $=$＂e＂THEN
$\operatorname{FOR}$ i $=1 \mathrm{TO} \mathrm{n}$
IF $x(i)=1$ THEN onigin $=1$ year（i）
NEXT i
trendx $=$（yea－origin）＊ $1 E+(m o n t-1)$
trend（1）$=$（amonth＋bmonth＊ 5 （ 5 ＋（bmonth＊trencts）
forecast $(1)=$ trencl $(1)$＊incex（mont）／a Qu

## ELSE

FOR $i=1 \mathrm{TO} n$
IF $x(i)=Q$ THEN origin $=\operatorname{year}(i)$
NEXT i

```
    #1, TAR(ES); "TAELE OF FERCENTAGES"
    #1, TAR(ES); "......................................................
    :b=G
    f=1 TOE
    k=1\
OR i = a TO b
    PRINT #1, TAB(k); amont$(i):
        k=k+1Q
NEXT i
R i=1 TO n
    k=10
RINT #1, TAE(E); year(i);
GOR j = a TO b
    PRINT #1, TAB(K); cm(i, j);
    k=k+1Q
NEXT j
<7 i
=a+6:b=b + E:FRTNT #1, % FRINT #2,
Tf
T #1, : PRTNT #1, TAE(3З); "SEASONAL. INDEX"
T #1, TAR(33); "-......................................"
T #1, TAB(3E); "MONTH"; TAE{44); "TNDEX"
T #1; TAB(3`); ".............""; TAR(44); "................"
i = 1 TO 1E
INT #1, TAB(3E); amont$(i); TAE(4E); inclex(i)
i
T #1, : FRINT #1,
    PRINT #\, TAB(E1); " FORECASTS FOR LE CONGECUTIUE MONTHS"
    PRINT 非, TAB(E|);
PRINT #1, TAR(こ\Xi); yea; TAR(3B); amontw(mont); TAR(53); forecast{1)
FOR i = E TO dE
    mont = mont + 1
        IF mont > ,IE THEN
            mont = mont - 1E
                yea = yea + &
    END IF
    trend(i) = trend(i - 1) + bmonth
    Forecast(i) == tmend(i) * index(mont) / 1.QQ
        FRINT #1, TAR(已J); yea; TAE(3S); amont$(mont); TAB(SZ); Forecast{i)
NEXT i
```

|  | ORIGINAL VALUES |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | jan | feb | mar | apr. | may | jun |
| 1990 | 245201 | 262334 | 293333 | 223145 | 244335 | 223123 |
| 1991 | 236330 | 251312 | 272211 | 243146 | 213116 | 201116 |
| 1992 | 208172 | 207113 | 198174 | 182243 | 178625 | 162116 |
| 1993 | 205488 | 228010 | 269995 | 237441 | 170162 | 202325 |
| 1994 | 199965 | 120111 | 199320 | 180615 | 185554 | 157101 |
| 1995 | 158407 | 131631 | 216783 | 206377 | 202525 | 145165 |
| 1996 | 171236 | 13.9876 | 240765 | 119786 | 211887 | 142234 |
|  | jul | aug | sep | oct | nov | dec |
| 1990 | 209876 | 200987 | 176543 | 211234 | 243213 | 254349 |
| 1991 | 182213 | 173211 | 163111 | 183123 | 213114 | 231322 |
| 1992 | 173251 | 171121 | 163311 | 182149 | 200133 | 213341 |
| 1993 | 155645 | 133417 | 166459 | 212133 | 204871 | 220320 |
| 1994 | 97214 | 70402 | 129420 | 132444 | 206481 | 174849 |
| 1995 | 128820 | 155429 | 21315 | 68833 | 94326 | 140385 |
| 1996 | 105666 | 143879 | 187654 | 129876 | 139871 | 149826 |

TABLE OF TREND ANALYSTS

| $X$ | $Y$ | $X Y$ | $X X$ |
| ---: | :--- | :--- | :--- |
| -3 | 2787673 | -8363019 | 9 |
| -2 | 2563325 | -5126650 | 4 |
| -1 | 2239749 | -2239749 | 1 |
| 0 | 2406266 | 0 | 0 |
| 1 | 1853476 | 1853476 | 1 |
| 2 | 1669996 | 3339992 | 4 |
| 3 | 1882556 | 5647668 | 9 |
| total | $1.540304 \mathrm{E}+07$ | -4888282 | 28 |

For the annual equation
Intercept $=2200435$
Slope $=-174581.5$

For the monthly equation
Intercept $=183369.5$
Slope $=-1212.372$

| YEAR | MONTH | DATA | 12-MTH M.T | 2 - MTH M.T OF C4 | 12 - MTH CMA |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1990 | jan | 245201 | 0 | 0 | 0 |
| 1990 | feb | 262334 | 0 | 0 | 0 |
| 1990 | mar | 293333 | 0 | 0 | 0 |
| 1990 | apr | 223145 | 0 | 0 | 0 |
| 1990 | may | 244335 | 0 | 0 | 0 |
| 1990 | jun | 223123 | 0 | 0 | 0 |
| 1990 | jul | 209876 | 2787673 | 5566475 | 231936.5 |
| 1990 | aug | 200987 | 2778802 | 5546582 | 231107.6 |
| 1990 | sep | 176543 | 2767780 | 5514438 | 229768.3 |
| 1990 | oct | 211234 | 2746658 | 5513317 | 229721.5 |
| 1990 | nov | 243213 | 2766659 | 5502099 | 229254.1 |
| 1990 | dec | 254349 | 2735440 | 5448873 | 227036.4 |
| 1991 | jan | 236330 | 2713433 | 5399203 | 224966.8 |
| 1991 | feb | 251312 | 2685770 | 5343764 | 222656.8 |
| 1991 | mar | 272211 | 2657994 | 5302556 | 220939.8 |
| 1991 | apr | 243146 | 2644562 | 5261013 | 219208.9 |
| 1991 | may | 213116 | 2616451 | 5202803 | 216783.5 |
| 1991 | jun | 201116 | 2586352 | 5149677 | 214569.9 |
| 1991 | jul | 182213 | 2563325 | 5098492 | 212437.2 |
| 1991 | aug | 173211 | 2535167 | 5026135 | 209422.3 |
| 1991 | sep | 163111 | 2490968 | 4907899 | 204495.8 |
| 1991 | oct | 183.123 | 2416931 | 4772959 | 198873.3 |
| 1991 | nov | 213114 | 2356028 | 4677565 | 194898.5 |
| 1991 | dec | 231322 | 2321537 | 4604074 | 191836.4 |
| 1992 | jan | 208172 | 2282537 | 4556112 | 189838 |
| 1992 | feb | 207113 | 2273575 | 4545060 | 189377.5 |
| 1992 | mar | 198174 | 2271485 | 4543170 | 189298.8 |
| 1992 | apr | 182243 | 2271685 | 4542396 | 189266.5 |
| 1992 | may | 178625 | 2270711 | 4528441 | 188685 |
| 1992 | jun | 162116 | 2257730 | 4497479 | 187395 |
| 1992 | jul | 173251 | 2239749 | $\cdots 4476814$ | 186533.9 |
| 1992 | aug | 171121 | 2237065 | 4495027 | 187292.8 |
| 1992 | sep | 163311 | 2257962 | 4587745 | 191156 |
| 1992 | oct | 182149 | 2329783 | 4714764 | $196448.5 *$ |
| 1992 | nov | 200133 | 2384981 | 4761499 | 198395.8 |
| 1992 | dec | 213341 | 2376518 | 4793245 | 199718.5 |
| 1993 | jan | 205488 | 2416727 | 4815848 | 200660.3 |
| 1993 | feb | 228010 | 2399121 | 4760538 | 198355.8 |
| 1993 | mar | 269995 | 2361417 | 4725982 | 196915.9 |
| 1993 | apr | 237441 | 2364565 | 4759114 | 198296.4 |
| 1993 | may | 170162 | 2394549 | 4793836 | 199743.2 |
| 1993 | jun | 202325 | 2399287 | 4805553 | 200231.4 |
| 1993 | jul | 155645 | 2406266 | 4807009 | 200292 |
| 1993 | aug | 133417 | 2400743 | 4693587 | 195566.1 |
| 1993 | sep | 166459 | 2292844 | 4515013 | 188125.5 |
| 1993 | oct | 212133 | 2222169 | 4387512 | 182813 |
| 1993 | nov | 204871 | 2165343 | 4346078 | 181086.6 |
| 1993 | dec | 220320 | 2180735 | 4316246 | 179843.6 |
| 1994 | jan | 199965 | 2135511 | 4212591 | 175524.6 |
| 1994 | feb | 120111 | 2077080 | 4091145 | 170464.4 |
| 1994 | mar | 199320 | 2014065 | 3991091 | 166295.5 |
| 1994 | apr | 180615 | 1977026 | 3874363 | 161431.8 |
| 1994 | may | 185554 | 1897337 | 3796284 | 158178.5 |
| 1994 | jun | 157101 | 1898947 | 3752423 | 156351 |
| 1994 | jul | 97214 | 1853476 | 3665394 | 152724.8 |
| 1994 | aug | 70402 | 1811918 | 3635356 | 151473.2 |
| 1994 | sep | 129420 | 1823438 | 3664339 | 152680.8 |


| 19y4 | oct | 132444 | 1840901 | 3707564 | 154481.8 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1994 | nov | 206481 | 1866663 | 3750297 | 156262.4 |
| 1994 | dec | 174849 | 1883634 | 3755332 | 156472.2 |
| 1995 | jan | 158407 | 1871698 | 3775002 | 157291.8 |
| 1995 | feb | 131631 | 1903304 | 3891635 | 162151.5 |
| 1995 | mar | 216783 | 1988331 | 3868557 | 161189.9 |
| 1995 | apr | 206377 | 1880226 | 3696841 | 154035 |
| 1995 | may | 202525 | 1816615 | 3521075 | 146711.5 |
| 1995 | jun | 145165 | 1704460 | 3374456 | 140602.3 |
| 1995 | jul | 128820 | 1669996 | 3352821 | 139700.9 |
| 1995 | aug | 155429 | 1682825 | 3373895 | 140579 |
| 1995 | sep | 21315 | 1691070 | 3406122 | 141921.8 |
| 1995 | oct | 68833 | 1715052 | 3343513 | 139313 |
| 1995 | nov | 94326 | 1628461 | 3266284 | 136095.2 |
| 1995 | dec | 140385 | 1637823 | 3272715 | 136363.1 |
| 1996 | jan | 171236 | 1634892 | 3246630 | 135276.3 |
| 1996 | feb | 139876 | 1611738 | 3211926 | 133830.3 |
| 1996 | mar | 240765 | 1600188 | 3366715 | 140279.8 |
| 1996 | apr | 119786 | 1766527 | 3594097 | 149754 |
| 1996 | may | 211887 | 1827570 | 3700685 | 154195.2 |
| 1996 | jun | 142234 | 1873115 | 3755671 | 156486.3 |
| 1996 | jul | 105666 | 1882556 | 0 | 0 |
| 1996 | aug | 143879 | 0 | 0 | 0 |
| 1996 | sep | 187654 | 0 | 0 | 0 |
| 1996 | oct | 129876 | 0 | 0 | 0 |
| 1996 | nov | 139871 | 0 | 0 | 0 |

TABLE OF PERCENTAGES

1990
1991
1992
1993
1994
1995
1996

1990
1991
1992
1993
1994
1995 1996

3707564 3750297 3755332 3775002 3891635 3868557 3696841 3521075 74456 3373895 3406122 3266284 3272715 3246630 3366715 3594097 3700685 3755671

0

| jan | feb | mar | apr | may | jun |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 | 0 | 0 |
| 105.0511 | 112.8697 | 123.2059 | 110.9198 | 98.30824 | 93.72984 |
| 109.6577 | 109.3652 | 104.6885 | 96.28909 | 94.66834 | 86.51034 |
| 102.4059 | 114.95 | 137.1118 | 119.7404 | 85.1904 | 101.0456 |
| 113.9242 | 70.46106 | 119.859 | 111.8832 | 117.3067 | 100.4797 |
| 100.709 | 81.17781 | 134.4892 | 133.9805 | 138.0431 | 103.2451 |
| 126.5825 | 104.5175 | 171.632 | 79.98849 | 137.4148 | 90.8923 |
|  |  |  |  |  |  |
| jul | aug | sep | oct | nov | dec |
| 90.48858 | 86.96686 | 76.83524 | 91.95219 | 106.0888 | 112.0301 |
| 85.77265 | 82.70896 | 79.76252 | 92.08024 | 109.3461 | 120.5829 |
| 92.87908 | 91.3655 | 85.43334 | 92.72099 | 100.8756 | 106.8208 |
| 77.70903 | 68.22092 | 88.48293 | 116.0382 | 113.1343 | 122.5065 |
| 63.65308 | 46.4782 | 84.76508 | 85.73435 | 132.1374 | 111.7445 |
| 92.2113 | 110.5635 | 15.01884 | 49.40887 | 69.30885 | 102.9494 |
| 0 | 0 | 0 | 0 | 0 | 0 |


| MONTH | INDEX |
| :---: | :---: |
| jan | 109.7664 |
| feb | 98.93047 |
| mar | 131.8848 |
| apr | 108.8445 |
| may | 111.8675 |
| jun | 96.0229 |
| jul | 83.81974 |
| aug | 81.08366 |
| sep | 71.74553 |
| oct | 88.02497 |
| nov | 105.1913 |
| dec | 112.8183 |

FORECASTS FOR 12 CONSECUTIVE MONTHS

| 1999 | jan | 112781.5 |
| :--- | :--- | :--- |
| 1999 | feb | 100448.5 |
| 1999 | mar | 132309.5 |
| 1999 | apr | 107875.5 |
| 1999 | may | 109515.3 |
| 1999 | jun | 92839.7 |
| 1999 | jul | 80024.88 |
| 1999 | aug | 76429.63 |
| 1999 | sep | 66757.66 |
| 1999 | oct | 80838.14 |
| 1999 | nov | 95327.63 |
| 1999 | dec | 100871.6 |

